WORK PACKAGE 2 : Design and simulation activities

DELIVERABLE D2.4

CNT based antenna design report

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## WORK PACKAGE 2: Design Activities

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1 INTRODUCTION

Introduction: Despite several international laboratories have theoretically studied the possibility to use nanotubes as antenna in different frequency domains such as THz, GHz, and optics. No experimental demonstration has been performed to the best of our knowledge. Before going through the physics of nano-antenna, we briefly introduce separately the basics of antennas and then of nanotubes/nanowires. Thus, we will go from the macro wire antenna model to the nano wire antenna model and review the similar and different parameters between the both scales.

Basics of wire antenna theory: Wire antennas are the oldest and most versatile antennas suited for various applications. It is a simple device to understand most of the radiation mechanism and the dipole structure simplification of radiating elements. The typical configuration is made up of two conductor wires, with a length of λ/2, as shown in the Figure 1.

The current distribution in the conductor wires (right side of Figure 1) can be considered in one dimension, due to the geometry (usually the z axis direction). This is the time variation of the current distribution that will generate a radiated electromagnetic field in the surrounding space. Maxwell's equations lead to the relation between the current variation I(z) and the radiated field Eθ in the far field space:

\[ \eta \frac{\partial I(z)}{\partial t} = jkE_\theta \]

Where η is the characteristic impedance of free space, k the constant propagation, l the dipole length, r and θ the radius and elevation angle coordinates. The 3-D emission pattern is said to be omni-directional because it only depends on θ. Figure 2 shows the typical radiation pattern of a wire antenna in a plane containing z-axis.

Along with the radiation pattern is a set of other key parameters that are used to quantify an antenna and its performances:

- The input impedance is the impedance the power input circuit will have to match in order to transmit the maximum power to the radiating device.
- The gain is the ratio of intensity, in a given direction, to the radiation intensity that would be obtained if the power accepted by the antenna was radiated isotropically. The radiation intensity corresponding to the isotropically radiated power is equal to the input power accepted by the antenna divided by 4π.
- The directivity is the ratio of the radiation intensity in a given direction from the antenna to the radiation intensity average over all directions.

Figure 1: Current distribution and free-space radiated field of a half-wavelength nano-dipole  
Figure 2: E-plane typical wire antenna pattern
The radiation efficiency which is the ratio of the radiated power over the accepted power and is a dimensionless combined factor of both the conduction efficiency (losses through metal conduction) and dielectric efficiency (losses through propagation in dielectric space).

**Basics of linear elements in the nanometric scale:** Size reduction toward nanometric scale changes the electromagnetic properties of the conducting elements. When a wire is fabricated whose cross-sectional dimension is comparable to the quantum mechanical (Fermi) wavelength of the electron, the wire forms essentially a single-mode waveguide for the electron waves. Then, in a one-dimensional conductor such as a nanotube, the electrons are only free to move along the length of the wire, and not in the transverse direction. Therefore the current distribution is effectively one-dimensional. In addition to the electron transport occurring in only one dimension, we also have two more important effects, large resistance and large inductance.

While copper is typically used in applications where high conductivity is required, it does not maintain its bulk conductivity when scaled to nanometer dimensions\(^{15}\). In contrast, nanotubes have better conductivity than copper when scaled to their diameter. It has recently been showed\(^ {13}\) that the dc resistance per unit length of a single-walled carbon nanotube at room temperature is about 6 kΩ/µm. A copper wire with the same diameter (1.5 nm) would have an even higher resistance per unit length. This resistance per unit length is quite large compared to the characteristic impedance of free space, as well as typical radiation resistances in traditional antennas. Therefore, it cannot be neglected. Recently it has been proven that the ac and dc resistances are the same for a nanotube up to about 10 GHz\(^ {14}\). However, these high impedances could be significantly reduced towards the 50 Ω if instead of resistive contact between the CNT and the dielectric substrate a capacitive contact is used\(^ {18}\). This means that between the metallic contact and CNT a thin dielectric is introduced. This particular configuration of the contact i.e. metal/dielectric/nanotube means that in parallel with the 6.5 kΩ resistance will be a capacitor with the overall effect of reducing the impedance of the CNT. Thus, the nano T/R module could work at impedance which is nearly of 50 Ω conferring compatibility with exiting wireless systems.

The distributed magnetic inductance and electrostatic capacitance on a two-wire transmission line gives rise to a wave-velocity that is typically in the order of the speed of light. However, in a carbon nanotube, there is another inductance, due to the kinetic energy of the electrons. Numerically, this inductance is typically 10,000 larger than the magnetic inductance, and so it dominates\(^ {15, 16, 17, 18}\). This large inductance causes the nanotube to behave as a quantum transmission line for RF voltages. The characteristic impedance of this line is in the range of several kΩ. In addition, the wavelength is about 50 to 100 times smaller than the free space wavelength for a given frequency\(^ {1, 2}\). This dramatically changes the current distribution compared to a thin-wire macro antenna, and must be accounted for. The conductivities of nano-tube and metallic wires are different because in a metallic wire the charges are relatively free of movement. This flux of charge is concentrated on the surface of the conductor in what is called the “conductivity skin depth”. Due to nano-tube special structures as shown in figure 3, there is very little possibilities for electron to move in the same manner as in a macro metal wire. In case of nanotubes, the electron movement is made by ballistic transport through the nanotubes with path length of about 100nm in the tubular structure\(^ {19}\) or via tunneling across gaps\(^ {20}\) with an associated high tunneling resistance.

*Figure 3: (a) Cut-out part of a monolayer termed graphene. (b) Single-walled carbon nanotube. (c) Multi-walled carbon nanotube, where several carbon nanotubes are nested concentrically.*
Following in the particular electrical properties of the nanotubes are the quantum and electrostatic capacitances. For a macro metal wire an electrostatic capacitance can be defined between the wire and a ground plane, capacitance that can be approximated by a 1-D model when the distance between the wire and the ground is larger than the length of the wire. This approximate value is $50 \text{ aF} \cdot \text{µm}^{-1}$ \cite{15,16}. In the case of a carbon nano-tube, which can be assimilated to a quantum 1-D electron gas, due to quantum physics properties, an electron can only be added under specific conditions and this leads to an average 1-D quantum capacitance of $100 \text{ aF} \cdot \text{µm}^{-1}$ \cite{15,16}.

The next issue deal with the wave velocity in a carbon nano-tube, as was already said previously. This wave velocity is lower than in a macro wire antenna. Experiment and theoretical calculations have shown that this wave velocity was in the order of the Fermi velocity ($v_F$) rather than the speed of light. For a carbon nanotube the propagation velocity is about $6.2 \times 0.02 \text{ c}$. The last issue deal with the characteristic impedance and the damping mechanisms associated with the carbon nanotube. Considering the kinetic inductance and the quantum capacitance, the characteristic impedance is equal to the quantum resistance which is $\Omega \approx \frac{kC_L}{QK^6}$. Due to the small size of the structures, damping need to be considered as well and is so far represented as a distributed resistance per unit of length.

Nano-antennas: It ensues from these electrical properties of the nano-tube the theoretical behavior of a nano-tube antenna. These characteristics are the same ones we acknowledge for a macro antenna but with very different values.

The first and most apparent change in characteristics is the wave propagation velocity and the resonance velocity. In a macro model, the resonance wave velocity is equal to the speed of light, in a nanotube antenna it goes otherwise. As was stated earlier, the wave propagation velocity in a nanotube transmission line is already $0.02 \text{ c}$, when used as a resonant dipole, the wave resonance in the nanotube can be associated with plasmons by the transmission line developed in \cite{2}, where the propagation velocity of the antenna was found to be $v_p = 3v_F = 0.01 \text{ c}$. Yet this is only a theoretical rough approximation of the reality. Further calculation and experiment give value around $0.015 \text{ c}$ and $0.017 \text{ c}$. This difference in wave resonance propagation velocity is illustrated in Figure 4, next, by the difference in current distribution along an antenna of same length for a given frequency.

The second characteristic to change is the input impedance. As a macro antenna, this impedance was around $50 \Omega \pm 50 \%$, as a nanotube antenna, this input impedance is approximately equivalent to the quantum resistance of the carbon nanotube, around $12.6 \text{ kΩ}$. This is a basic characteristic impedance that will characterize all nanosized transmitting device, whether a transmission line or an antenna or any other component.

Next we will consider the current distribution. On a carbon nanotube of length equal to 0.01 to 0.02 the length of a metal wire antenna for the same frequency of use, the current distribution will be similar on the nanotube and on the metal wire, thus leading to the same current equation that will also lead to the same radiation pattern from Figure 2. Contrarily to the macro metal wire antenna, the

Figure 4: Current distribution for nanotube versus wire antennas of the same length.
carbon nanotube antenna will show a very low gain due to a low radiation efficiency compared to macro antennas\cite{1}. It will not be unusual to obtain antenna whose radiation efficiency in dB is in the range –60 to -70 dB\cite{2}. This is due to the damping phenomena that is present at these dimensions which was presented previously.

Last is a new feature that needs to be considered for the nano-tube and was not present at the macro scale is the low-level frequency damping. It was calculated and experimented that under frequency around 50GHz, the nanotube antenna damping will prevent any radiation thus only working properly usually from 60/100 GHz to higher frequencies\cite{1,2,21}. This low level limit in frequency radiation is linked to the relaxation frequency that can vary from 50 GHz to 1 THz\cite{22}.

Some recent papers deal with theoretical study of the interaction of one-dimensional electronic systems with microwave radiation, leading to a quantitative theory of CNT antenna performance\cite{23}. Since CNTs can be grown having lengths on the order of cm, and can be metallic, a natural topic is to consider CNTs for centimeter and millimeter wave antenna applications. In fact, one of the technical issues that scientists have to face to bring the nanotechnologies to reality is the communication and data exchange between the nano-sized devices or organisms and the macro-world. Using nano-antennas based on CNTs for wireless communications could solve this issue. In this project, we propose to study theoretically and experimentally the feasibility of such a nano-antenna in the high frequency domain (2-80 GHz) with return loss $S_{11}$ of -30 dB.

The possibility to create CNT antenna array will also be investigated with the particular emphasis to integrate these antennas with the CNT FET and CNT switch forming the wireless interface for the T/R module. Due to the small radiation power from a single CNT, CNT antenna array's will be necessary in some applications in order to achieve enough radiated power. The CNT can be fabricated together forming form sub-array’s where the radiated power will be the sum of these sub-array’s. Different concepts for the antenna array will be investigated as well as the effect of the CNT itself (i.e. CNT diameter, CNT length and inter-CNT distances). Comparisons with conventional antennas like microstrip antennas will also be done.

The CNT antenna for microwaves should have a length of few up to tens of millimeters. This means that the CNT antenna will not stand vertically as in the case of optical antennas, but horizontally. To implement a CNT antenna will require a combination of micromachining techniques and nanotechnologies to implement a CNT antenna.

Using the same concept other configurations will be studied such as rectangular spirals, or even a CNT based Yagi antenna.

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<td>-30 dB</td>
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<tr>
<td>Bandwidth</td>
<td>Not measured</td>
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<tr>
<td>Beam width</td>
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<td>&lt;70 degrees</td>
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Table 1: CNT antennas baselines and NANO-RF goals.

2 CNT MATERIAL PROPERTIES FOR ANTENNA APPLICATIONS

For antenna design prospects, specific material electromagnetic properties must be identified such as conductivity, permittivity and an associated propagation constant of a microwave signal transmitted through this nanomaterial. Multiphysics and multiscale modelling procedures are then accessible from
material properties understanding to device design. In this part, most important helpful theoretical CNT material properties are summarized in order to achieve antenna design based on this new material. Design work is executed in coordination with WP3 in which experimental values extraction is forecast for modelling tools refinement.

A. CNT NATURE VS CHIRALITY

CNT electronic properties are defined from a graphene monolayer where carbon atoms are spatially distributed as a periodic honeywell geometry (Fig.5). From growth process, carbon nanotubes are formed as an axial graphene sheet rolling following a chiral vector $C_t$ relying on two arbitrary vectors $a_1$ and $a_2$ separated by an angle $\theta$ as

$$C_t = a_1 \times a_2$$

The two $n$ and $m$ integers define then the chirality of a carbon nanotube by imposing direction of $C_t$, which can be identified as zigzag, armchair or strongly chiral. These $(n,m)$ integers pair also determine the CNT electronic nature, as a semiconducting or metallic nanomaterial if $m = 3N$ and $n = 0$, $m = n$, $2m + n = 3N$ in a zigzag, armchair or chiral configuration respectively.

Carbon nanotube diameter is also related to these $(n,m)$ integers pair as expressed in Equ.3.

$$a_0 = \sqrt{3} \cdot a_{c-c} = 2.42 \text{ nm}$$

B. SW/MW CNT ENERGY BAND DIAGRAMS

Optical absorption and emission properties of SW/MW CNTs rely on their energy band diagram characterized by unconventional conduction and valence bands profiles with discretized energy spikes values known as Van Hove singularities pairs (Fig. 2). The energy separation between the highest valence band and the lowest conduction band singularities is given by Equ.4a – 4b where $a_{c-c}$ is the lattice distance of two carbon atoms (equal to 0.142 nm) and $d_t$ is the SW CNT diameter.

$$E_{c-t}^n(d) = 2a_{c-c}y_0/d_t$$

$$E_{c-t}^n(d) = 6a_{c-c}y_0/d_t$$

As shown in Fig. 2, the first Van Hove peaks determine the authorized transfert energy for both semiconductor and metallic SW CNT from a global energy band diagram study. Thus optical transitions occur at $E_{c-t}^n(d)$, $2E_{c-t}^n(d)$, $4E_{c-t}^n(d)$, $6E_{c-t}^n(d)$ ... energy levels, which are determined experimentally from fluorescence and emission spectra from photoluminescence or
electroluminescence and/or absorption spectra from Raman spectroscopy. These energy levels strongly depend on tube diameter and chirality vector.

Figure 6: Energy levels as a function of Density of States (DOS) for semiconducting (left) and metallic (right) SW CNTs.

C. CNT Conductivity vs Chirality

For CNT-based antenna design, metallic behaviour of CNT nanomaterial is chosen to obtain a material with conductivity level comparable to classical metals. Because of exceptional material aspect ratio, material conductivity have been redefined by theoretical studies of electron transport in cylindrical surfaces depending on chirality vector $\mathbf{C}$.

Dynamic conductivity of a carbon nanotube represents a macroscopic quantity relating the disturbance of electron flow along the nanotube due to an incremental temporal variation in the applied electric field along it. For conventional carbon nanotube structures, the length of the nanotube is much greater than its circumference. Thus, for most practical cases, it is assumed that the equivalent current along the surface of the nanotube is transversely symmetric and parallel to the axis of the nanotube.

Depending on chiral vector, specific complex conductivity equations (Equ. 5a-5b-5c) have been defined leading to extraordinary conductive behaviour of a metallic CNT compared to a classical metal. Indeed, in association with a positive real part, identification of a negative imaginary part fulfills the inductive behaviour of such a material, which can be easily implemented in electromagnetic software.

$$\sigma_{zz\text{chiral}} = -j\frac{8\pi e^2\gamma_0\sqrt{3}}{h^2\sqrt{m^2+n^2(\omega-j\nu)+mn}} \text{ with } 2m+n=3N \quad (5a)$$

$$\sigma_{zz\text{armchair}} = -j\frac{8\pi e^2\gamma_0}{mh^2(\omega-j\nu)} \text{ with } m=n \quad (5b)$$

$$\sigma_{zz\text{zigzag}} = -j\frac{8\pi e^2\gamma_0\sqrt{3}}{mh^2(\omega-j\nu)} \text{ with } m=3N \text{ and } n=0 \quad (5c)$$

Interesting electromagnetic properties from CNTs formed in a chiral configuration ($2m+n = 3N$, $N$ as an integer) are expected as reported in Fig. 7 where a high positive real part ($10^5$ S/m) and negative imaginary part ($-10^6$ S/m) of conductivity is predicted from theory in a DC-100GHz frequency band.
3 STATE OF THE ART OF CNT MATERIAL MODELLING TOOLS FOR ANTENNA APPLICATIONS

Carbon nanotubes are becoming an extraordinary nanomaterial for antenna design, thanks its atomic structure and spatial geometry. For radiation properties purpose, some antenna parameters must be strongly considered from material point of view such as:

- Lineic inductance/capacitance in order to define the efficient dimension of a LC resonant cell
- Dynamic permittivity which allows the definition of plasma resonance
- Band diagram and work function definition in a metallic behaviour to identify efficient contact type with microwave electrode access to match input impedance.

Different modelling tools using electrical or electromagnetic properties of individual Carbon nanotubes have been studied in order to predict radiation properties of unique or bundle of CNTs. This part summarizes all accessible modelling tools for CNT-based antenna design.

From material point of view, CNT-based nano antennas design activity needs to take into account SW/MW CNTs electrical characteristics in order to fulfill radiative behaviour predictions in microwave frequency domain. In this project, three modeling procedures, implemented in existing commercial microwave circuit design softwares, are reported:

- Individual electrical modeling which can be developed in commercial analytical/electrical softwares

Figure 7: Dynamic conductivity as a function of frequency of a metallic chiral CNT (with m and n equal to 1)
- Electromagnetic modeling as a bulk material defined by its electromagnetic parameters to achieved a completed 3D definition of radiative elements
- A Transmission-line equivalent model represented by its lineic resistance, inductance, capacitance and conductance parameters
- A metamaterial approach for dimensions and density influence effect on electromagnetic properties

A. INDIVIDUAL CNT /CNT BUNDLE ELECTRICAL MODELLING FROM ELECTRON FLUID MODEL OF CARBON NANOTUBE TRANSMISSION LINE

From first procedure, SW CNTs modeling relies on a comprehensive electrical homemade model [1] defined by a lineic series kinetic inductance $L_k$ and resistance $R_{CNT}$, and a $(R_c, C_{el})$ parallel cell for each metal/CNT contact as shown in Fig. 8. Electrical parameters expressions and values are reported in Table 2.

![Figure 8 : Individual CNT electrical modeling](image)

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<td>16 nH/µm (calculated) $^{24}$&lt;br&gt;10-40 nH/µm (measured) $^{25}$</td>
<td>$\frac{h}{2a^2v_F}$</td>
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<td>$R_{CNT}$</td>
<td>6.5 kΩ/µm calculated $^{[26]}$</td>
<td>$\frac{h}{4e^2}$</td>
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<td>$C_{el}$</td>
<td>0.2-0.7 fF/µm measured in DC $^{24}$&lt;br&gt;10-50 fF/µm measured up to 4 GHz $^{[28]}$</td>
<td>NA</td>
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<tr>
<td>$R_c$</td>
<td>Up to 25 kΩ $^{[24]}$</td>
<td>Dependence with metal type choice and then contact type (ohmic/Schottky)</td>
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Table 2 : Electrical parameters of SW CNTs
If CNTs bundles are considered, CNT-based nano antennas modelling can be also assumed by a parallel network connection of individual CNTs as defined in Fig.9. As the density knowledge of CNTs is critical, other modelling tools are necessary in a CNT bundle configuration.

**B. INDIVIDUAL CNT /CNT BUNDLE ELECTROMAGNETIC MODELING FROM SURFACE WAVE PROPAGATION**

The second modelling procedure (Fig.10) relies on the assumption that CNTs bundles are equivalent to a macroscopic material layer defined by its complex permittivity ($\varepsilon$), permeability ($\mu$) and conductivity ($\sigma$). These parameters are commonly determined by S-parameters measurements\(^{27}\). This modelling methodology offers flexibility in nano antenna design by use of 3D electromagnetic microwave software where microwave access design can be accurately defined referring to dedicated technological process.

It is interesting to note that the series elements of this equivalent distributed circuit of carbon nanotube can be directly obtained by using the equivalent surface conductivity of armchair carbon nanotube which is discussed in the previous section as follows:

**C. TRANSMISSION-LINE EQUIVALENT MODEL OF CNT BUNDLES**

The next competitive CNT modelling method suggests the equivalence between CNT bundles with a classical transmission line defined by a classical lineic equivalent circuit (Fig.11).

For this modelling tool, S-parameters matrix of CNTs bundles deposited between microwave accesses are converted into an ABCD matrix in order to extract constant propagation of signals $\gamma$ inside CNTs bundle and its equivalent impedance $Z$. From this model, lineic series resistance $R$ and inductance $L$ in parallel with shunt conductance $G$ and capacitance $C$ can be determined in frequency $^{28}$.

**D. METAMATERIAL APPROACH**

Due to periodicity and aspect ratio of CNT bundles, a metamaterial approach has been previously studied at UPMC. This new approach needs today to be validated by experimental results.

This last CNT modelling solution consists of defining CNT bundles as periodic conducting straight thin wires array with electromagnetic properties close to metamaterials $^{29}$. In this way, elementary wires are electrically defined with equivalent electrical circuit defined for individual CNTs (Fig.12, 13).
Figure 10: Electromagnetic equivalence of CNTs bundle and experimental results of permittivity in frequency\textsuperscript{27}

Figure 11: Transmission-line equivalence of CNTs bundle and experimental results of complex permittivity in frequency\textsuperscript{28}

Propagation constant and phase velocity calculations allows then frequency dispersion of such an array, for which forbidden frequency bands are identified as in fig.8. Parametric simulations are accessible in order to predict working frequency of CNT bundles for their use as nano emitters.
E. MATERIAL PARAMETERS CONSIDERATIONS FOR ANTENNA DESIGN

From theoretical results, specific material optimization work must be undertaken in order to match as close as possible to:
- A resonant input impedance with highest resistance and near-zero reactance value at frequency of emission
- The highest far-field emission gain
- A near zero input reflexion coefficient for impedance circuit matching to 50 Ohms
4 CNT-BASED ANTENNA TOPOLOGIES

This activity report summarizes CNT-based antenna design work relying on use of 3D FDTD parametric electromagnetic analysis from Ansys commercial software. The main scientific objective is to validate theoretical results on exceptional sub-wavelength radiation of such antenna topology with CNT material, by electromagnetic simulations. Free space (monopole/dipole) and integrated on usual substrate (quartz, Si) CNT-based antenna topologies have been investigated in order to validate potential antenna miniaturization by this innovative material thanks to the existence of a negative imaginary conductivity leading to high inductive behaviour compared to classical metals in microwave domain.

In coordination with NANO RF partnership available technological platforms to CNT growth, vertically-aligned MW CNT arrays organized in cylindrical bundles were considered in order to define a hollow wire-like dipole/monopole, into two electromagnetic environment such as:

- Free space environment
- Integrated technology

CNT-based antenna design optimizations are executed on microwave performances such as resonant frequency / frequency bandwidth, input impedance and E and H-plane radiation patterns. CNT-based radiating part is modelled by an exotic conductive tube with specific impedance and diameter defining then the vertical MW metallic CNT bundle.

From dynamic conductivity $\sigma_{zz}$ expression (Equ. XXX), MW CNT bundle modelling is assumed by an individual vacuum cylinder of arbitrary length $L$, radius $r$ and surface impedance $Z_s$ (Equ. 6). Negative imaginary part of $\sigma_{zz}$ implies then a positive reactance value at a pulsation $\omega$ confirming the expected inductive behaviour of MW CNTs. $Z_s$ complex value can be easily tuned through parametric simulations in order to achieve targeted microwave performances.

$$Z_s = \frac{i}{2\pi r \sigma_{zz}} = R_s + jL_s \omega$$  \hspace{1cm} (6)

For miniaturization purpose, this statement becomes crucial to shorten drastically the operational dipole/monopole length which must be typically equal to the wavelength $\lambda$ over 2 or 4 respectively in the case of a classical metallic wire.

A. FREE SPACE DIPOLE/MONOPOLE CONFIGURATION

a) Definition of a classical metallic wire dipole in free space environment
As a reference, a typical metallic wire with a length of 1.5 mm assuming then a theoretical resonant frequency of 100 GHz, and a radius of 10 µm has been modelled as a reference (Fig. 14). Expected efficient microwave performances in terms of return loss, input impedance and 3D radiation pattern have been successfully recovered.

b) Definition of a metallic tube dipole in free space environment
From this case study, dipole parameters modifications such as on the cylinder conductive characteristics have been operated by changing the metallic to dielectric ($\varepsilon_r$ equal to 1) wire and implementing a surface impedance on its external lateral surface with arbitrary resistance and reactance values. A metallic tube is then designed by imposing a resistance and reactance equal to zero.
D2.4 : CNT based antenna design report

Figure 14 : Free space dipole configuration of a metallic tube with very low real resistive surface (0.001 Ohm.cm2) - Working frequency around 100 GHz (92.8 GHz) with λ/2 = 1.5 mm

c) Parametric simulations of free space MW CNT-based dipole
First parametric simulations on surface impedance resistance and reactance reveal an efficient input impedance matching frequency tunability (Fig. 15) of tens of GHz if a high reactance value is introduced. In parallel, input impedance resonances appearance witnesses effective radiation at lower frequency, as reported in Table 3.

d) Optimized design for experimental demonstration
In coordination with WP2 and WP3, microwave mounting tests have been fabricated in order to determine experimentally effective radiation of monopole MW CNT bundles of 1 x 1 mm³ (Fig. 17), on doped Si substrate. S-parameters and radiation patterns measurements are under work.
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Table 3 : Matching and radiation frequencies of a conductive tube dipole in free space environment for different impedance surface $Z_s$.

Figure 15 : Far field 3D gain radiation pattern at 60 GHz (a) and 126.4 GHz (b) of a conductive tube with specific complex resistive surface ($Z_s = 0.001+j*10$ Ohm.m²) – (c) Associated antenna input impedance as a function of frequency (red curve: real part – purple curve: imaginary part) - Dipole length: 1.5 mm
Figure 16: Far field 3D gain radiation pattern at 53 GHz (a) a conductive tube with specific complex resistive surface ($Z_s = 0.001 + j 0.01 \text{ Ohm.m}^2$) – (b) Associated antenna input impedance as a function of frequency (red curve: real part – purple curve: imaginary part) - Dipole length: 1.5 mm.

Figure 17: First experimental microwave test structure configuration (c) of MW CNT bundle monopole on doped Si wafer (a) after wafer dicing/etching (TRT/MC2) and report on quartz substrate (b) implemented inside a protected microwave mounting with a 2,4 mm/50Ω coaxial access (with technical support of IEMN/MC2).
Figure 18: Example of a CNT-based dipole antenna integrated on quartz substrate: (a) 3D design – (b) Input complex impedance – (c) 3D radiation pattern

Figure 19: Example of a CNT-based dipole antenna integrated on quartz substrate: (a) Taper length influence from 150 to 250 um on Return loss in frequency – (b) Input impedance in frequency with a taper length of 150 um
B. CNT MONOPOLE INTEGRATION ON DIELECTRIC/SEMICONDUCTOR SUBSTRATE

a) Definition of selected antenna integrated technology
In order to design a CNT-based antenna in integrated technology, a CNT bundle monopole configuration has been selected. Regarding vertical CNT process constraints, coplanar technology have been preferred for 50 ohms microwave feeding circuit implementation on low permittivity dielectric substrate as reported in Fig. 18, 19.

b) First antenna design
For impedance matching, a tapered feeding transmission line has been designed between microwave input access and the vertical MW CNT bundle operating as a monopole. In this configuration, with respect to vertical CNT technological process constraints, effective sub-wavelength radiation performances are optimized from parametric simulations form design parameters such as taper line length and end width, ground plane dimensions and profile, CNT bundle length and diameter, CNT bundle complex surface impedance.

c) Electromagnetic simulations results
By assuming a CNT bundle monopole with tunable complex surface impedance, parametric simulations allows first radiation efficiency at frequencies around 10 GHz of the CNT-based monopole (Fig. 18). As reported in Fig. 19a, impedance access matching needs supplementary design optimization in order to maximize far field gain of the antenna, as reported in Fig.19b as taper length tuning allows minimization of return losses at very low frequency.

By tuning surface reactance of CNT bundle (20), simulations results predict an operational CNT-based monopole antenna at 4.8 GHz with a total gain of 7.2 dB (Fig. 21). CNT radiation contribution has been validated from electromagnetic simulations results from the same microwave circuit design without CNT bundle monopole delivering microwave radiation only by the tapered coplanar line with a gain of -8.9 dB at the same frequency of 4.8 GHz.
Figure 21: (a) 3D radiation pattern of a 750um-length CNT-based monopole antenna integrated on quartz substrate with a surface reaction of 0.301 Ω.m² – (b) Input resistance in the 1-50 GHz and (c) 50-150 GHz frequency bands
d) Design optimization

To achieve the highest microwave performances, further design optimization will be focused on ground plane topology and microwave access line profile.

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